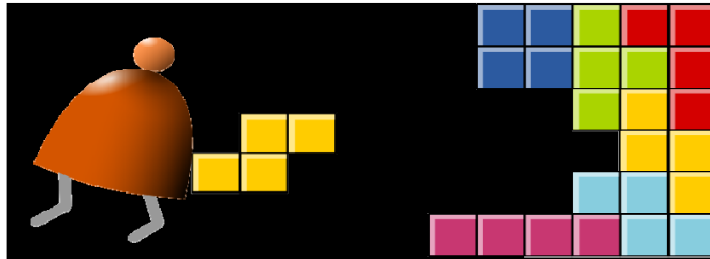


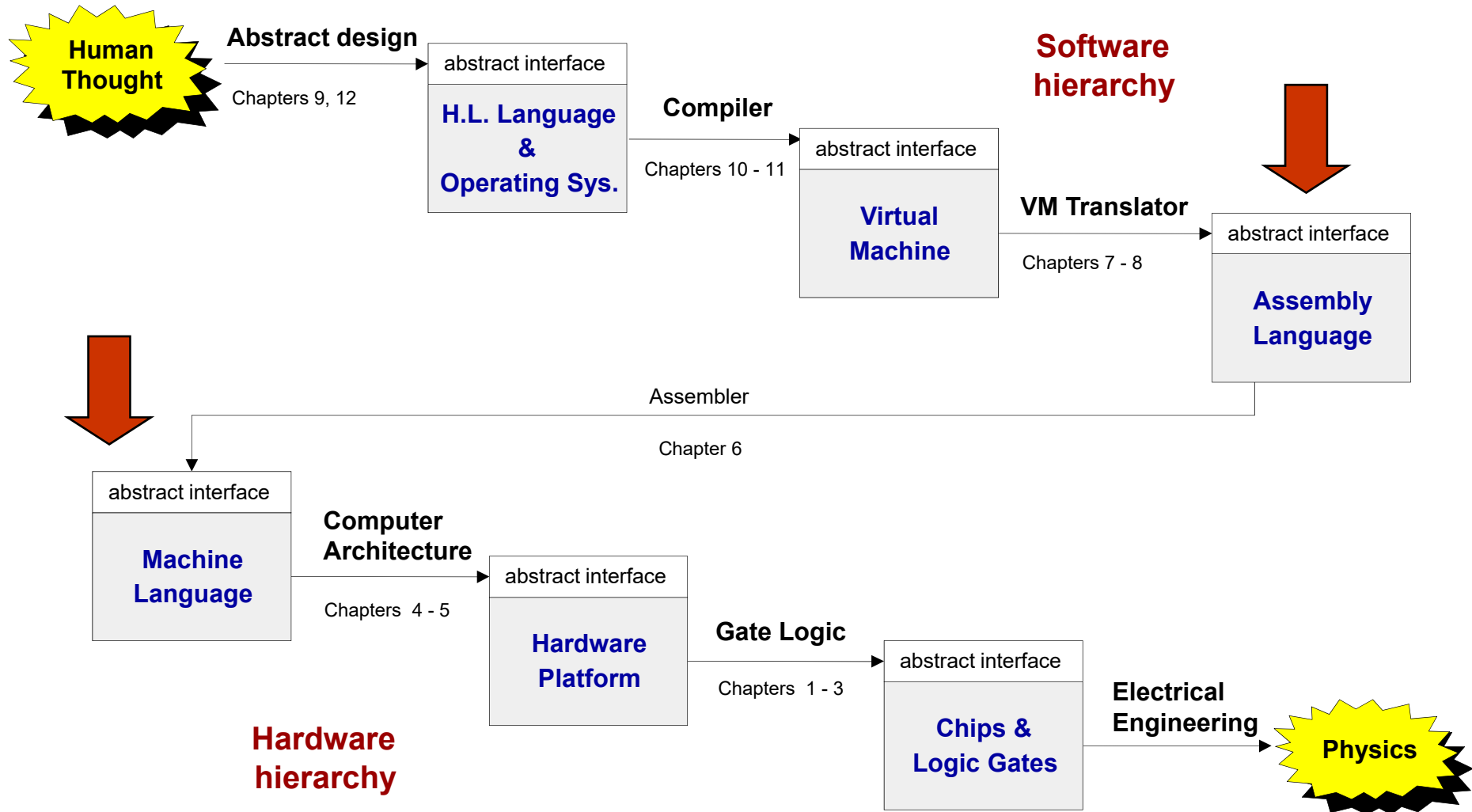
Machine (Assembly) Language



Building a Modern Computer From First Principles

www.nand2tetris.org

Where we are at:

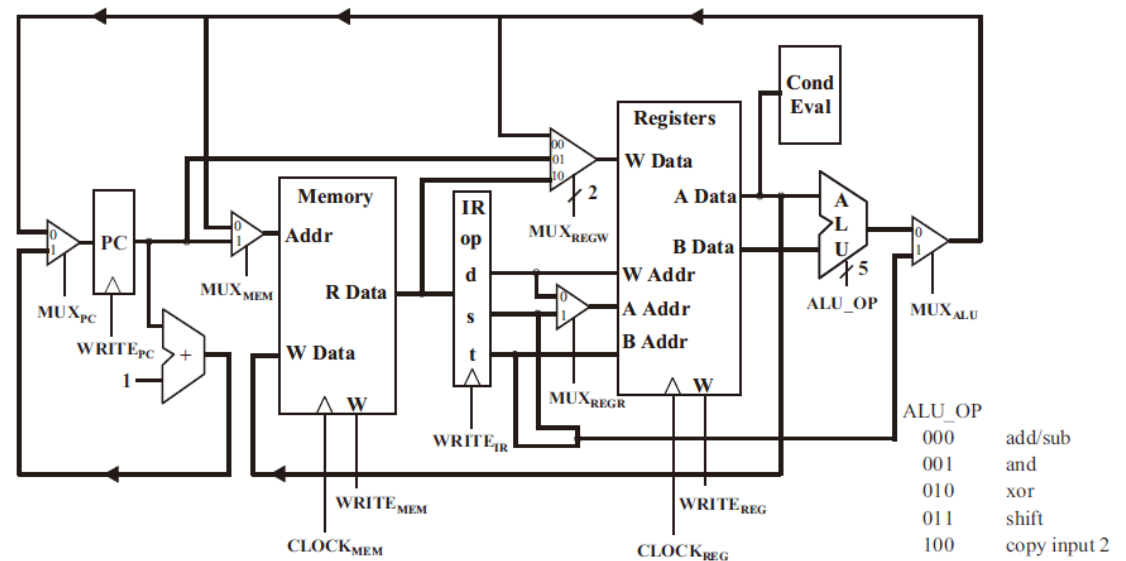


Machine language

Abstraction - implementation duality:

- Machine language (= instruction set) can be viewed as a programmer-oriented abstraction of the hardware platform
- The hardware platform can be viewed as a physical means for realizing the machine language abstraction

#	Operation	Fmt	Pseudocode
0:	halt	1	<code>exit(0)</code>
1:	add	1	<code>R[d] ← R[s] + R[t]</code>
2:	subtract	1	<code>R[d] ← R[s] - R[t]</code>
3:	and	1	<code>R[d] ← R[s] & R[t]</code>
4:	xor	1	<code>R[d] ← R[s] ^ R[t]</code>
5:	shift left	1	<code>R[d] ← R[s] << R[t]</code>
6:	shift right	1	<code>R[d] ← R[s] >> R[t]</code>
7:	load addr	2	<code>R[d] ← addr</code>
8:	load	2	<code>R[d] ← mem[addr]</code>
9:	store	2	<code>mem[addr] ← R[d]</code>
A:	load indirect	1	<code>R[d] ← mem[R[t]]</code>
B:	store indirect	1	<code>mem[R[t]] ← R[d]</code>
C:	branch zero	2	<code>if (R[d] == 0) pc ← addr</code>
D:	branch positive	2	<code>if (R[d] > 0) pc ← addr</code>
E:	jump register	1	<code>pc ← R[t]</code>
F:	jump and link	2	<code>R[d] ← pc; pc ← addr</code>



Machine language

Abstraction - implementation duality:

- Machine language (= instruction set) can be viewed as a programmer-oriented abstraction of the hardware platform
- The hardware platform can be viewed as a physical means for realizing the machine language abstraction

Another duality:

- Binary version: 0001 0001 0010 0011 (machine code)
- Symbolic version ADD R1, R2, R3 (assembly)

Machine language

Abstraction - implementation duality:

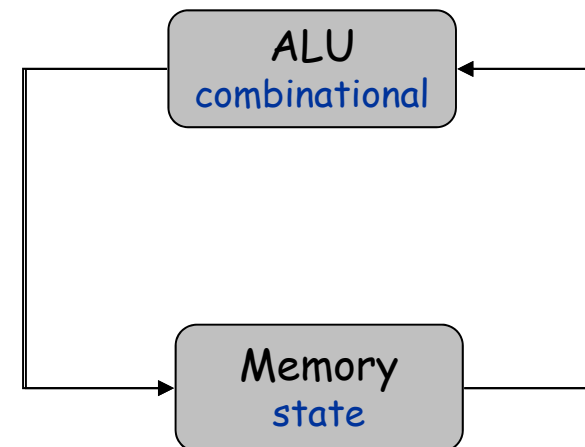
- Machine language (= instruction set) can be viewed as a programmer-oriented abstraction of the hardware platform
- The hardware platform can be viewed as a physical means for realizing the machine language abstraction

Another duality:

- Binary version
- Symbolic version

Loose definition:

- Machine language = an agreed-upon formalism for manipulating a memory using a processor and a set of registers
- Same spirit but different syntax across different hardware platforms.



Lecture plan

- Machine languages at a glance
- The Hack machine language:
 - Symbolic version
 - Binary version
- Perspective

(The assembler will be covered in chapter 6).

Typical machine language commands (3 types)

- ALU operations

- Memory access operations

(addressing mode: how to specify operands)

- Immediate addressing, LDA R1, 67 // R1=67
- Direct addressing, LD R1, 67 // R1=M[67]
- Indirect addressing, LDI R1, R2 // R1=M[R2]

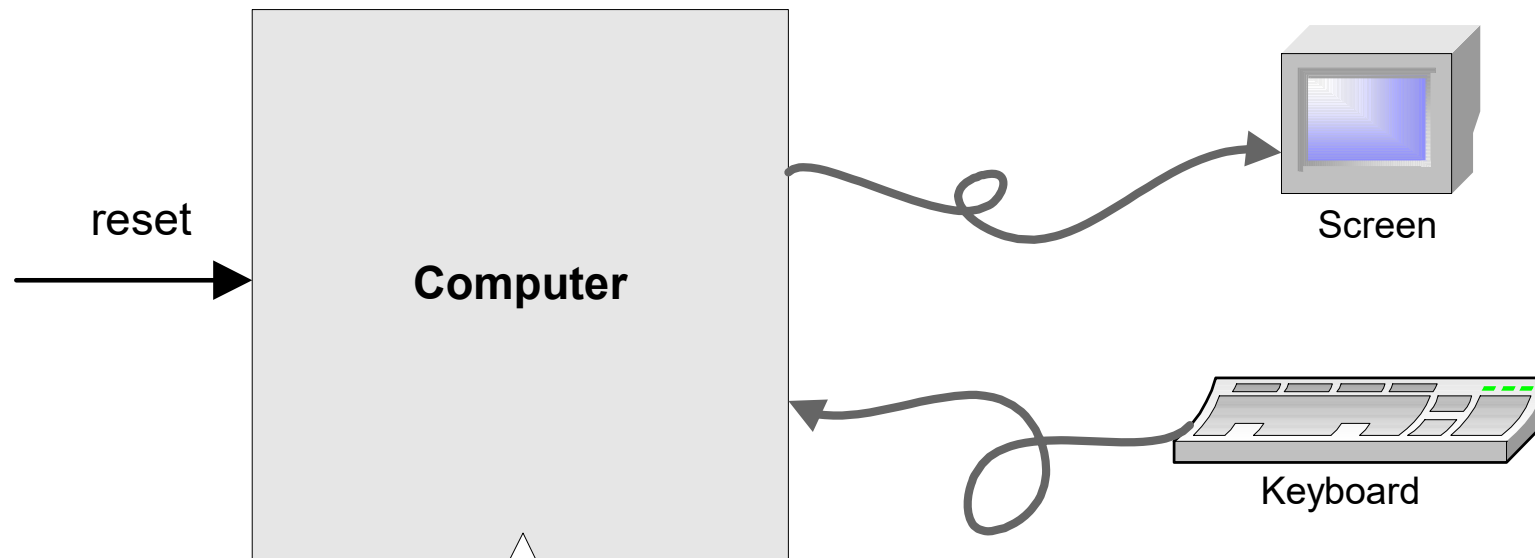
- Flow control operations

Typical machine language commands (a small sample)

```
// In what follows R1,R2,R3 are registers, PC is program counter,  
// and addr is some value.  
  
ADD R1,R2,R3      // R1 ← R2 + R3  
  
ADDI R1,R2,addr   // R1 ← R2 + addr  
  
AND R1,R1,R2      // R1 ← R1 and R2 (bit-wise)  
  
JMP addr          // PC ← addr  
  
JEQ R1,R2,addr    // IF R1 == R2 THEN PC ← addr ELSE PC++  
  
LOAD R1, addr     // R1 ← RAM[addr]  
  
STORE R1, addr    // RAM[addr] ← R1  
  
NOP               // Do nothing  
  
// Etc. - some 50-300 command variants
```


The Hack computer

A 16-bit machine consisting of the following elements:



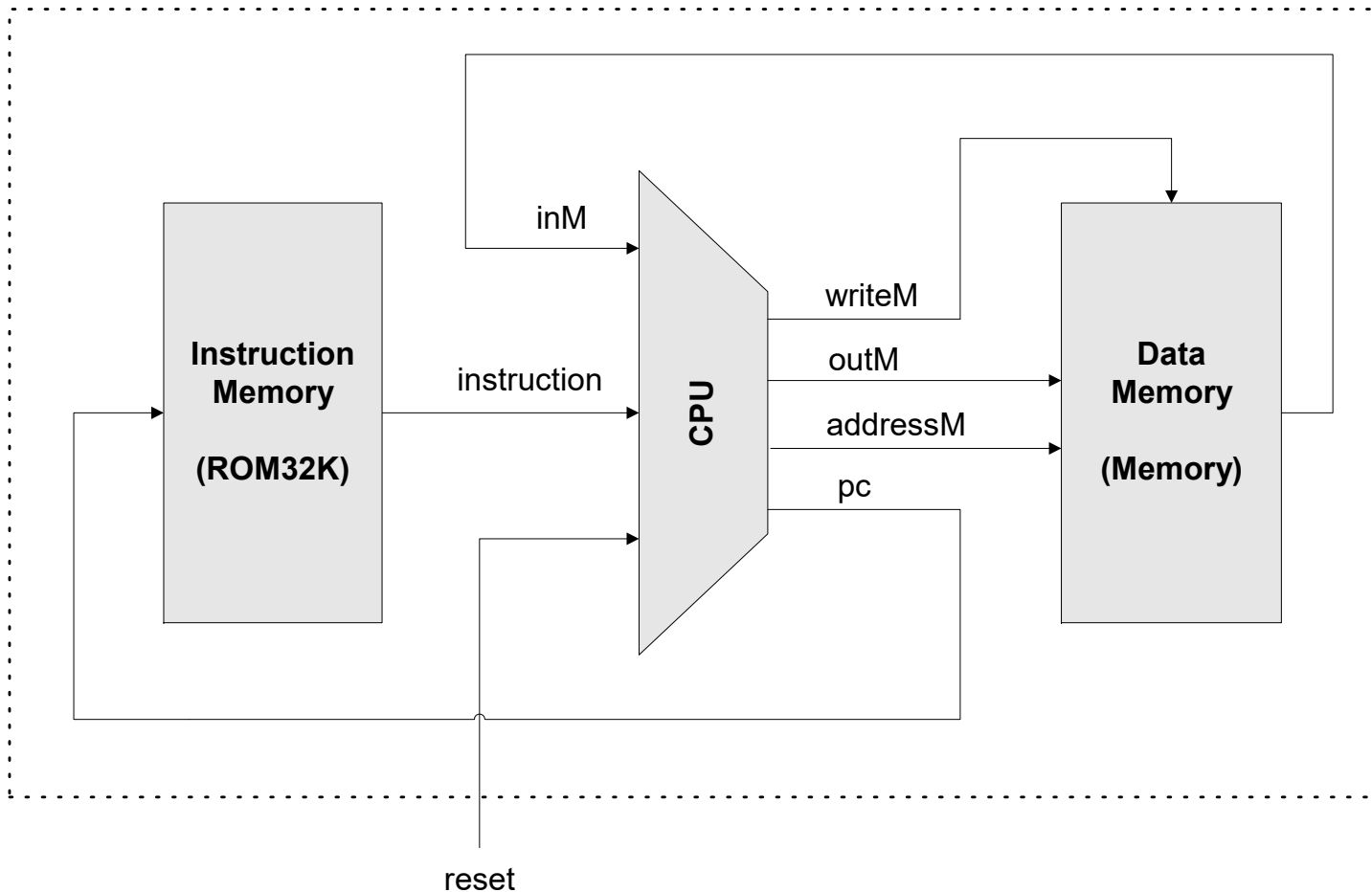
The Hack computer

- The ROM is loaded with a Hack program
- The reset button is pushed
- The program starts running



The Hack computer

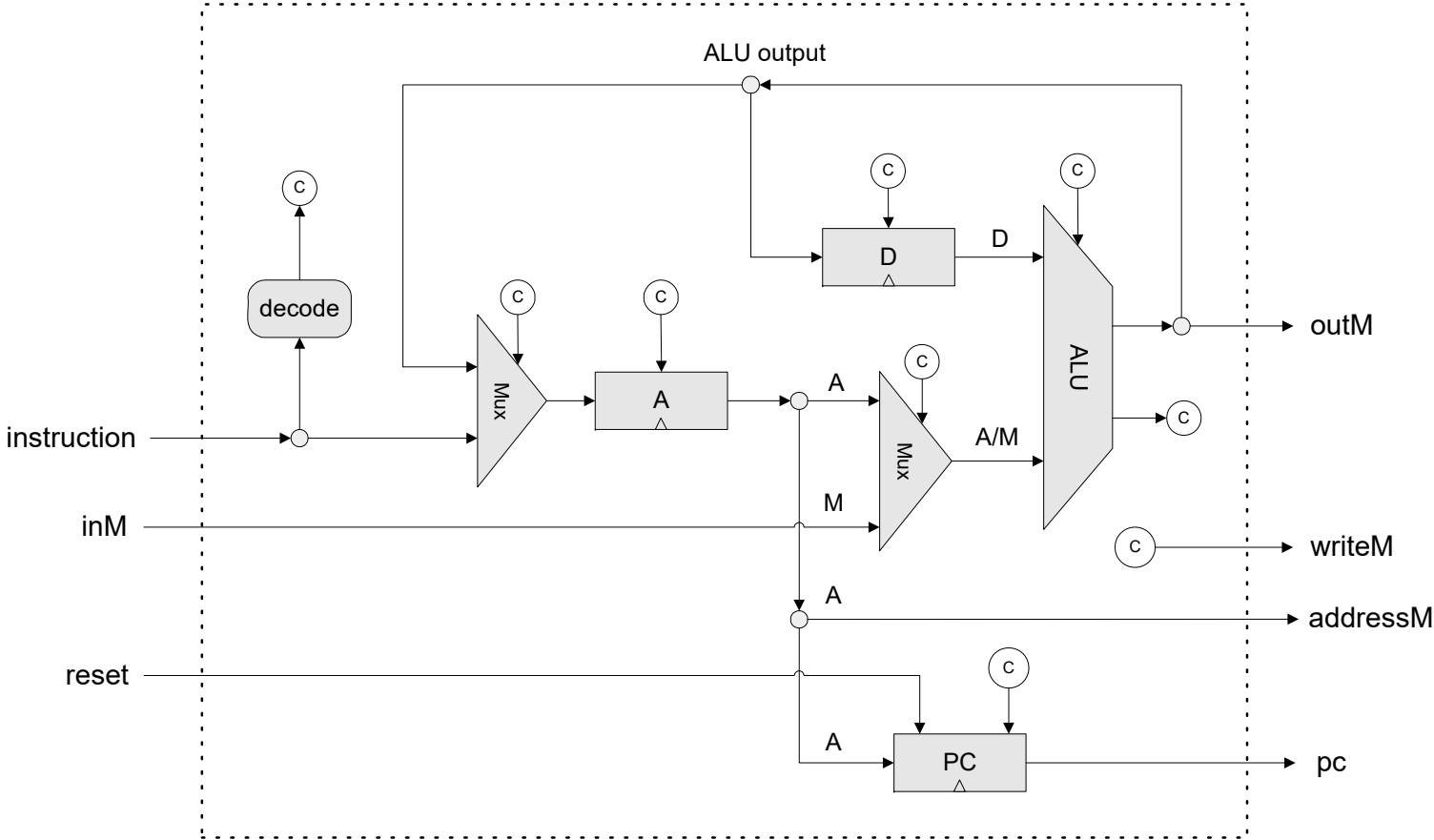
A 16-bit machine consisting of the following elements:



Both memory chips are 16-bit wide and have 15-bit address space.

The Hack computer (CPU)

A 16-bit machine consisting of the following elements:



The Hack computer

A 16-bit machine consisting of the following elements:

Data memory: **RAM** - an addressable sequence of registers

Instruction memory: **ROM** - an addressable sequence of registers

Registers: **D, A, M**, where **M** stands for **RAM[A]**

Processing: **ALU**, capable of computing various functions

Program counter: **PC**, holding an address

Control: The **ROM** is loaded with a sequence of 16-bit instructions, one per memory location, beginning at address 0. Fetch-execute cycle: later

Instruction set: Two instructions: **A**-instruction, **C**-instruction.

The A-instruction

```
@value // A ← value
```

Where *value* is either a number or a symbol referring to some number.

Why A-instruction?

In TOY, we store address in the instruction (fmt #2). But, it is impossible to pack a 15-bit address into a 16-bit instruction. So, we have the A-instruction for setting addresses if needed.

Example:

```
@21
```

Effect:

- Sets the A register to 21
- RAM[21] becomes the selected RAM register M

The A-instruction

```
@value // A ← value
```

Used for:

- Entering a constant value
(A = value)
- Selecting a RAM location
(register = RAM[A])
- Selecting a ROM location
(PC = A)

Coding example:

```
@17 // A = 17  
D = A // D = 17
```

```
@17 // A = 17  
D = M // D = RAM[17]  
M = -1 // RAM[17]=-1
```

```
@17 // A = 17  
JMP // fetch the instruction  
// stored in ROM[17]
```

The C-instruction

dest = comp ; jump

Both *dest* and *jump* are optional.

First, we compute something.

Next, optionally, we can store the result, or use it to jump to somewhere to continue the program execution.

comp:

0, 1, -1, D, A, !D, !A, -D, -A, D+1, A+1, D-1, A-1, D+A, D-A, A-D, D&A, D|A
M, !M, -M, M+1, M-1, D+M, D-M, M-D, D&M, D|M

dest: null, A, D, M, MD, AM, AD, AMD

jump: null, JGT, JEQ, JLT, JGE, JNE, JLE, JMP

Compare to zero. If the condition holds, jump to ROM[A]

The C-instruction

dest = comp ; jump

- Computes the value of comp
- Stores the result in dest
- If (the condition jump compares to zero is true), goto the instruction at ROM[A].

The C-instruction

dest = comp ; jump

comp:

0, 1, -1, D, A, !D, !A, -D, -A, D+1, A+1, D-1, A-1, D+A, D-A, A-D, D&A, D|A
M, !M, -M, M+1, M-1, D+M, D-M, M-D, D&M, D|M

dest: null, A, D, M, MD, AM, AD, AMD

jump: null, JGT, JEQ, JLT, JGE, JNE, JLE, JMP

Example: set the D register to -1

D = -1

Example: set RAM[300] to the value of the D register minus 1

@300

M = D-1

Example: if ((D-1) == 0) goto ROM[56]

@56

D-1; JEQ

Hack programming reference card

Hack commands:

A-command: `@value` // set A to value

C-command: `dest = comp ; jump` // `dest =` and `;jump`
// are optional

Where:

`comp` =

0 , 1 , -1 , D , A , !D , !A , -D , -A , D+1 , A+1 , D-1 , A-1 , D+A , D-A , A-D , D&A , D|A ,
M , !M , -M , M+1 , M-1 , D+M , D-M , M-D , D&M , D|M

`dest` = M, D, A, MD, AM, AD, AMD, or null

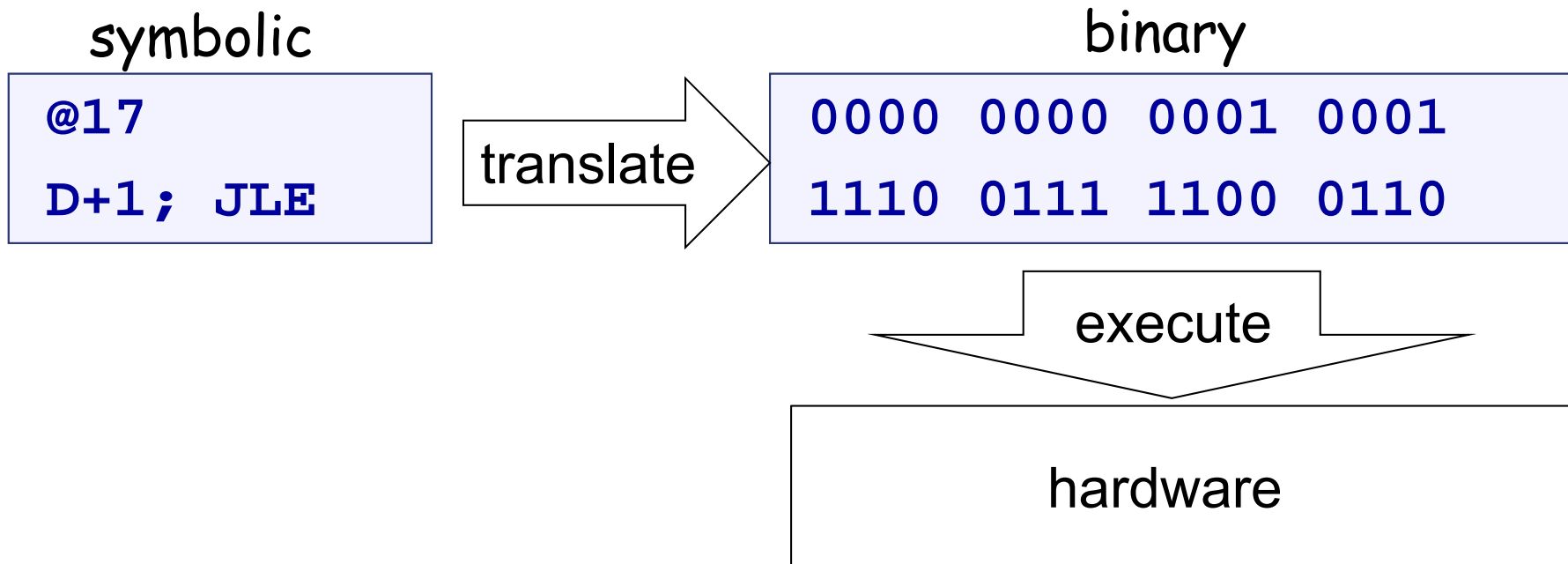
`jump` = JGT , JEQ , JGE , JLT , JNE , JLE , JMP, or null

In the command `dest = comp; jump`, the jump materializes if (`comp` `jump` 0) is true. For example, in `D=D+1,JLT`, we jump if `D+1 < 0`.

The Hack machine language

Two ways to express the same semantics:

- Binary code (machine language)
- Symbolic language (assembly)



The A-instruction

symbolic

`@value`

- *value* is a non-negative decimal number $\leq 2^{15}-1$ or
- A symbol referring to such a constant

binary

`0value`

- *value* is a 15-bit binary number

Example

`@21`

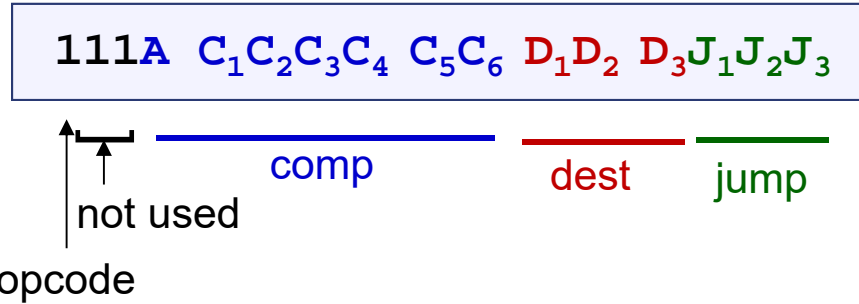
`0000 0000 0001 0101`

The C-instruction

symbolic

dest = comp ; jump

binary



The C-instruction

111A C₁C₂C₃C₄ C₅C₆ D₁D₂ D₃J₁J₂J₃

comp

dest

jump

(when a=0)	c1	c2	c3	c4	c5	c6	(when a=1)
<i>comp</i>							<i>comp</i>
0	1	0	1	0	1	0	
1	1	1	1	1	1	1	
-1	1	1	1	0	1	0	
D	0	0	1	1	0	0	
A	1	1	0	0	0	0	M
!D	0	0	1	1	0	1	
!A	1	1	0	0	0	1	!M
-D	0	0	1	1	1	1	
-A	1	1	0	0	1	1	-M
D+1	0	1	1	1	1	1	
A+1	1	1	0	1	1	1	M+1
D-1	0	0	1	1	1	0	
A-1	1	1	0	0	1	0	M-1
D+A	0	0	0	0	1	0	D+M
D-A	0	1	0	0	1	1	D-M
A-D	0	0	0	1	1	1	M-D
D&A	0	0	0	0	0	0	D&M
D A	0	1	0	1	0	1	D M

The C-instruction

111A C₁C₂C₃C₄ C₅C₆ D₁D₂ D₃J₁J₂J₃

comp

dest

jump

A	D	M		
d1	d2	d3	<i>Mnemonic</i>	<i>Destination (where to store the computed value)</i>
0	0	0	null	The value is not stored anywhere
0	0	1	M	Memory[A] (memory register addressed by A)
0	1	0	D	D register
0	1	1	MD	Memory[A] and D register
1	0	0	A	A register
1	0	1	AM	A register and Memory[A]
1	1	0	AD	A register and D register
1	1	1	AMD	A register, Memory[A], and D register

The C-instruction

111A $C_1C_2C_3C_4$ C_5C_6 D_1D_2 $D_3J_1J_2J_3$

comp

dest

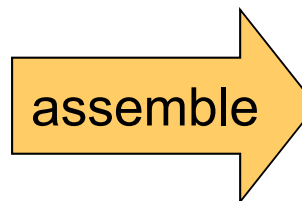
jump

j1 (<i>out</i> < 0)	j2 (<i>out</i> = 0)	j3 (<i>out</i> > 0)	Mnemonic	Effect
0	0	0	null	No jump
0	0	1	JGT	If <i>out</i> > 0 jump
0	1	0	JEQ	If <i>out</i> = 0 jump
0	1	1	JGE	If <i>out</i> ≥ 0 jump
1	0	0	JLT	If <i>out</i> < 0 jump
1	0	1	JNE	If <i>out</i> ≠ 0 jump
1	1	0	JLE	If <i>out</i> ≤ 0 jump
1	1	1	JMP	Jump

Hack assembly/machine language

Source code (example)

```
// Computes 1+...+RAM[0]
// And stored the sum in RAM[1]
    @i
    M=1 // i = 1
    @sum
    M=0 // sum = 0
(LLOOP)
    @i // if i>RAM[0] goto WRITE
    D=M
    @R0
    D=D-M
    @WRITE
    D;JGT
    @i // sum += i
    D=M
    @sum
    M=D+M
    @i // i++
    M=M+1
    @LOOP // goto LOOP
    0;JMP
(WRITE)
    @sum
    D=M
    @R1
    M=D // RAM[1] = the sum
(END)
    @END
    0;JMP
```



Hack assembler
or CPU emulator

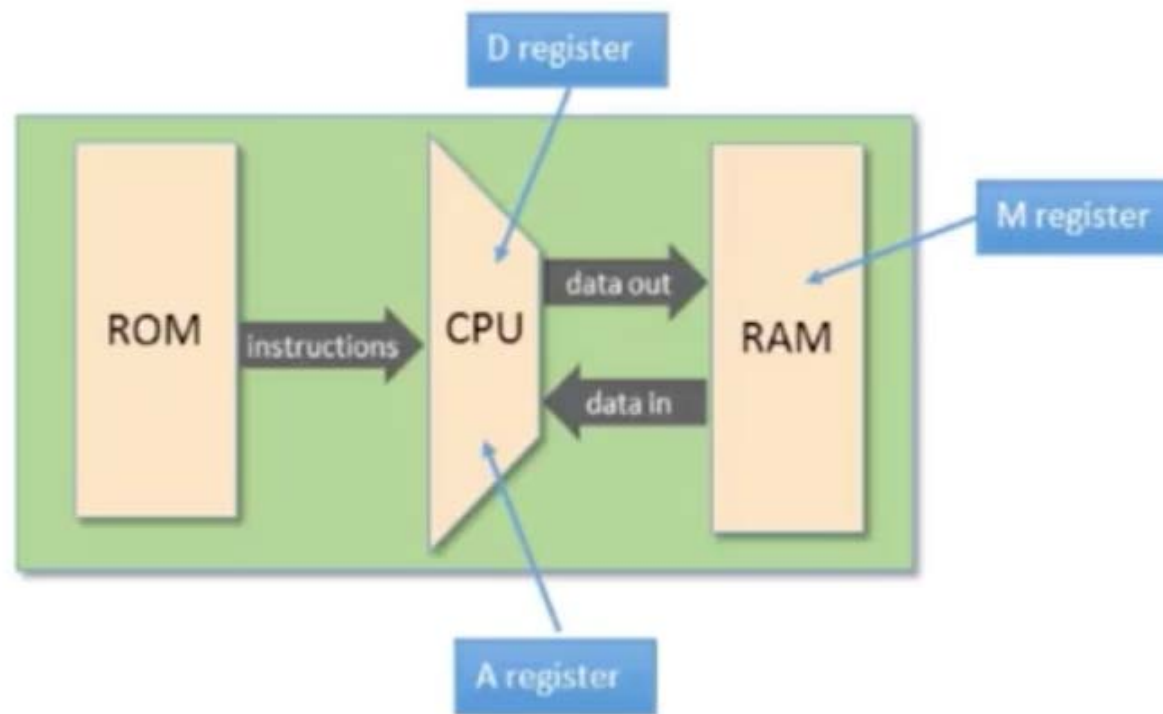
Target code

```
0000000000010000
1110111111001000
0000000000010001
1110101010001000
0000000000010000
1111110000010000
0000000000000000
1111010011010000
0000000000010010
1110001100000001
0000000000010000
1111110000010000
0000000000010001
1111000010001000
0000000000010000
1111110111001000
0000000000000100
1110101010000111
0000000000010001
1111110000010000
0000000000000001
1110001100001000
0000000000010110
1110101010000111
```

We will focus on writing the assembly code.

Working with registers and memory

- D: data register
- A: address/data register
- M: the currently selected memory cell, $M=RAM[A]$



Hack programming exercises

Exercise: Implement the following tasks using Hack commands:

1. Set `D` to `A-1`
2. Set both `A` and `D` to `A + 1`
3. Set `D` to `19`
4. `D++`
5. `D=RAM[17]`
6. Set `RAM[5034]` to `D - 1`
7. Set `RAM[53]` to `171`
8. Add `1` to `RAM[7]`,
and store the result in `D`.

Hack programming exercises

Exercise: Implement the following tasks using Hack commands:

1. Set D to A-1

2. Set both A and D to A + 1

3. Set D to 19

4. D++

5. D=RAM[17]

6. Set RAM[5034] to D - 1

7. Set RAM[53] to 171

8. Add 1 to RAM[7],
and store the result in D.

1. D = A-1

2. AD=A+1

3. @19

D=A

4. D=D+1

5. @17

D=M

6. @5034

M=D-1

7. @171

D=A

@53

M=D

8. @7

D=M+1

A simple program: add two numbers (demo)

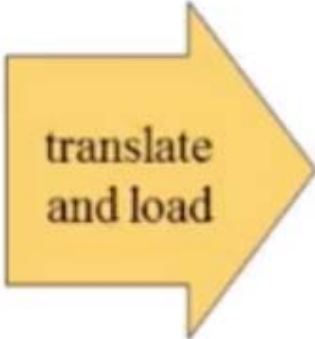
Hack assembly code

```
// Program: Add2.asm
// Computes: RAM[2] = RAM[0] + RAM[1]
// Usage: put values in RAM[0], RAM[1]

0 @0
1 D=M // D = RAM[0]

2 @1
3 D=D+M // D = D + RAM[1]

4 @2
5 M=D // RAM[2] = D
```



White space is ignored

Memory (ROM)

0	@0
1	D=M
2	@1
3	D=D+M
4	@2
5	M=D
6	
7	
8	
9	
10	symbolic view
11	
12	
13	
14	
15	
	⋮
32767	

Terminate properly

- To avoid malicious code, you could terminate your program with an infinite loop, such as

@6

0; JMP

Built-in symbols

symbol	value
R0	0
R1	1
R2	2
...	...
R15	15
SCREEN	16384
KBD	24576

symbol	value
SP	0
LCL	1
ARG	2
THIS	3
THAT	4

- R0, R1, ..., R15 : virtual registers
- SCREEN and KBD : base address of I/O memory maps
- Others: used in the implementation of the Hack Virtual Machine
- Note that Hack assembler is case-sensitive, R5 != r5

Branching

```
// Program: branch.asm
// if R0>0
//   R1=1
// else
//   R1=0
```

Branching

```
// Program: branch.asm
// if R0>0
//   R1=1
// else
//   R1=0

    @R0
    D=M          // D=RAM[0]

    @8
    D; JGT      // If R0>0 goto 8

    @R1
    M=0         // R1=0
    @10
    0; JMP      // go to end

    @R1
    M=1         // R1=1

    @10
    0; JMP
```

Branching

```
// Program: branch.asm
// if R0>0
//   R1=1
// else
//   R1=0

    @R0
    D=M          // D=RAM[0]

    @8
    D; JGT      // If R0>0 goto 8

    @R1
    M=0         // R1=0
    @10
    0; JMP      // go to end

    @R1
    M=1         // R1=1

    @10
    0; JMP
```

Branching with labels

```

// Program: branch.asm
// if R0>0
//   R1=1
// else
//   R1=0

    @R0
    D=M           // D=RAM[0]

    @POSTIVE ← refer a label
    D; JGT       // If R0>0 goto 8

    @R1
    M=0         // R1=0
    @END
    0; JMP      // go to end
(POSTIVE) ← declare a label
    @R1
    M=1         // R1=1
(END)
    @10
    0; JMP

```

0	@0
1	D=M
2	@8
3	D;JGT
4	@1
5	M=0
6	@10
7	0;JMP
8	@1
9	M=1
10	@10
11	0; JMP
12	
13	
14	
15	
16	

IF logic – Hack style

High level:

```
if condition {  
    code block 1  
} else {  
    code block 2  
}  
code block 3
```

Hack convention:

- ❑ True is represented by -1
- ❑ False is represented by 0

Hack:

```
D ← condition  
@IF_TRUE  
D;JEQ  
code block 2  
@END  
0;JMP  
(IF_TRUE)  
code block 1  
(END)  
code block 3
```

Coding examples (practice)

Exercise: Implement the following tasks using Hack commands:

1. goto 50
2. if D==0 goto 112
3. if D<9 goto 507
4. if RAM[12] > 0 goto 50
5. if sum>0 goto END
6. if x[i]<=0 goto NEXT.

Coding examples (practice)

Exercise: Implement the following tasks using Hack commands:

1. goto 50

1. @50

5. @sum

0; JMP

D=M

2. if D==0 goto 112

2. @112

@END

3. if D<9 goto 507

D; JEQ

D: JGT

4. if RAM[12] > 0 goto 50

3. @9

6. @i

D=D-A

D=M

5. if sum>0 goto END

@507

@x

D; JLT

A=D+M

6. if x[i]<=0 goto NEXT.

4. @12

D=M

D=M

@NEXT

@50

D; JLE

D; JGT

variables

```
// Program: swap.asm  
// temp = R1  
// R1 = R0  
// R0 = temp
```


variables

```
// Program: swap.asm
// temp = R1
// R1 = R0
// R0 = temp

    @R1
    D=M
    @temp
    M=D           // temp = R1

    @R0
    D=M
    @R1
    M=D           // R1 = temp

    @temp
    D=M
    @R0
    M=D           // R0 = temp

(END)
    @END
    0;JMP
```

- When a symbol is encountered, the assembler looks up a symbol table
- If it is a new label, assign a number (address of the next available memory cell) to it.
- For this example, temp is assigned with 16.
- If the symbol exists, replace it with the number recorded in the table.
- With symbols and labels, the program is easier to read and debug. Also, it can be relocated.

Hack program (exercise)

Exercise: Implement the following tasks
using Hack commands:

1. `sum = 0`

2. `j = j + 1`

3. `q = sum + 12 - j`

4. `arr[3] = -1`

5. `arr[j] = 0`

6. `arr[j] = 17`

Hack program (exercise)

Exercise: Implement the following tasks using Hack commands:

1. <code>sum = 0</code>	1. <code>@sum</code> <code>M=0</code>	4. <code>@arr</code> <code>D=M</code>	6. <code>@j</code> <code>D=M</code>
2. <code>j = j + 1</code>	2. <code>@j</code> <code>M=M+1</code>	<code>@3</code> <code>A=D+A</code>	<code>@arr</code> <code>D=D+M</code>
3. <code>q = sum + 12 - j</code>	3. <code>@sum</code> <code>D=M</code>	<code>M=-1</code>	<code>@ptr</code> <code>M=D</code>
4. <code>arr[3] = -1</code>	<code>@12</code> <code>D=D+A</code>	5. <code>@j</code> <code>D=M</code>	<code>@17</code> <code>D=A</code>
5. <code>arr[j] = 0</code>	<code>@j</code> <code>D=D-M</code>	<code>@arr</code> <code>A=D+M</code>	<code>@ptr</code> <code>A=M</code>
6. <code>arr[j] = 17</code>	<code>@q</code> <code>M=D</code>	<code>M=0</code>	<code>M=D</code>

WHILE logic – Hack style

High level:

```
while condition {  
    code block 1  
}  
Code block 2
```

Hack:

```
(LOOP)  
    D ← condition  
    @END  
    D;JNE  
    code block 1  
    @LOOP  
    0;JMP  
(END)  
    code block 2
```

Hack convention:

- ❑ True is represented by -1
- ❑ False is represented by 0

Complete program example

C language code:

```
// Adds 1+...+100.  
int i = 1;  
int sum = 0;  
while (i <= 100){  
    sum += i;  
    i++;  
}
```

Hack assembly convention:

- ❑ Variables: lower-case
- ❑ Labels: upper-case
- ❑ Commands: upper-case

Complete program example

Pseudo code:

```
i = 1;
sum = 0;
LOOP:
    if (i>100) goto END
    sum += i;
    i++;
    goto LOOP
END:
```

Hack assembly convention:

- Variables: lower-case
- Labels: upper-case
- Commands: upper-case

Demo
CPU emulator

Hack assembly code:

```
// Adds 1+...+100.
    @i        // i refers to some RAM location
    M=1       // i=1
    @sum      // sum refers to some RAM location
    M=0       // sum=0
(LLOOP)
    @i
    D=M       // D = i
    @100
    D=D-A     // D = i - 100
    @END
    D;JGT     // If (i-100) > 0 goto END
    @i
    D=M       // D = i
    @sum
    M=D+M     // sum += i
    @i
    M=M+1     // i++
    @LLOOP
    0;JMP     // Got LOOP
( END )
    @END
    0;JMP     // Infinite loop
```

Example

```
// for (i=0; i<n; i++)  
//     arr[i] = -1;
```

Pseudo code:

Example

```
// for (i=0; i<n; i++)  
//     arr[i] = -1;
```

Pseudo code:

```
i = 0
```

```
(LOOP)
```

```
    if (i-n)>=0 goto END
```

```
    arr[i] = -1
```

```
    i++
```

```
    goto LOOP
```

```
(END)
```


Example

```
// for (i=0; i<n; i++)
//     arr[i] = -1;

    @i
    M=0
(LLOOP)
    @i
    D=M
    @n
    D=D-M
    @END
    D; JGE

    @arr
    D=M
    @i
    A=D+M
    M=-1

    @i
    M=M+1

    @LOOP
    0; JMP
(END)
```

Pseudo code:

```
i = 0

(LLOOP)
    if (i-n)>=0 goto END
    arr[i] = -1
    i++
    goto LOOP
(END)
```

Perspective

- Hack is a simple machine language
- User friendly syntax: `D=D+A` instead of `ADD D,D,A`
- Hack is a “ $\frac{1}{2}$ -address machine”: any operation that needs to operate on the RAM must be specified using two commands: an `A`-command to address the RAM, and a subsequent `C`-command to operate on it
- A Macro-language can be easily developed
 - `D=D+M[XXX] => @XXX` followed by `D=D+M`
 - `GOTO YYY => @YYY` followed by `0; JMP`
- A Hack assembler is needed and will be discussed and developed later in the course.